

**Math 527 - Homotopy Theory**  
**Spring 2013**  
**Homework 11, Lecture 4/1**

**Problem 1.** Show that a path-connected space is weakly equivalent to a product of Eilenberg-MacLane spaces if and only if it admits a Postnikov tower of principal fibrations with trivial  $k$ -invariants (all of them).

**Note.** Here, we follow Hatcher's convention that the  $k$ -invariants are used to build the Postnikov tower of  $X$  starting from  $P_1X$  and not  $P_0X$ . In other words, by "Postnikov tower of principal fibrations", we mean that the maps  $P_nX \rightarrow P_{n-1}X$  are principal fibrations for all  $n \geq 2$ . Using  $n \geq 1$  instead would force  $\pi_1X$  to be abelian.